

Calculus Section 4.1 Trig Antiderivatives

-Use indefinite integral notation for antiderivatives.

-Use basic integration rules to find antiderivatives.

Homework: page 251 #'s 24 - 32

Trig antiderivatives are the inverse of trig derivatives.

Trig derivatives and antiderivatives:

$$\frac{dy}{dx} \sin x = \cos x$$

$$\frac{dy}{dx} \cos x = -\sin x$$

$$\frac{dy}{dx} \tan x = \sec^2 x$$

$$\frac{dy}{dx} \cot x = -\csc^2 x$$

$$\frac{dy}{dx} \sec x = \sec x \tan x$$

$$\frac{dy}{dx} \csc x = -\csc x \cot x$$

$$\int \cos x dx = \sin x + C$$

$$\int \sin x dx = -\cos x + C$$

$$\int \sec^2 x dx = \tan x + C$$

$$\int \csc^2 x dx = -\cot x + C$$

$$\int \sec x \tan x dx = \sec x + C$$

$$\int \csc x \cot x dx = -\csc x + C$$

Examples)

$$\int \frac{\sin x}{\cos^2 x} dx$$

$$\int \tan x \sec x dx$$

$$\boxed{\sec x + C}$$

$$\int \cot x \sin x dx$$

$$\int \frac{\cos x}{\sin x} \sin x dx$$

$$\int \cos x dx$$

$$\boxed{\sin x + C}$$

$$\int (\sec^2 x + \sin x - \csc^2 x) dx$$

$$\boxed{\tan x - \cos x + \cot x + C}$$

$$\int -(\sec x \tan x - \cos x) dx$$

$$\int (-\sec x \tan x + \cos x) dx$$

$$\boxed{-\sec x + \sin x + C}$$